## Multiple Linear Regression Exercise

1) The following data were taken from the personnel records of 12 clerks (all male) working at an insurance company. Each record contains information on the number of days absent during the year, the duration of employment with the company, and a measure of attitude towards the company (part of a clinical interview with the company's psychologist). The attitude scale ranges from 1 (extremely favorable) to 13 (extremely unfavorable).

| Clerk | Days Absent | Attitude | Experience |
| :---: | :---: | :---: | :---: |
| 1 | 1 | 1 | 1 |
| 2 | 0 | 2 | 1 |
| 3 | 1 | 2 | 2 |
| 4 | 4 | 3 | 2 |
| 5 | 3 | 5 | 4 |
| 6 | 2 | 5 | 6 |
| 7 | 5 | 6 | 5 |
| 8 | 6 | 7 | 4 |
| 9 | 9 | 10 | 8 |
| 10 | 13 | 11 | 7 |
| 11 | 15 | 11 | 9 |
| 12 | 16 | 12 | 10 |
|  |  |  |  |
| Mean | 6.25 | 6.25 | $\mathbf{4 . 9 2}$ |
| Std. Dev. | $\mathbf{5 . 6 8}$ | $\mathbf{3 . 9 3}$ | $\mathbf{3 . 1 2}$ |


|  | Correlations |  |  |
| :---: | :---: | :---: | :---: |
|  | Days Absent | Attitude | Experience |
| Days Absent | 1 | .950 | .890 |
| Attitude | .950 | 1 | .951 |
| Experience | .890 | .951 | 1 |

2) Suppose you believe new employees have fewer absences than more experienced employees. Write the coefficients for the leastsquares regression line in the space below. Interpret the coefficients and calculate the coefficient of determination.

Absences $=$ $\qquad$ $+$ $\qquad$ (experience) $\qquad$
$R^{2}=$
3) You want to determine if experience is a significant predictor of absences. First, write out the full and reduced models you wish to compare. Then, run the omnibus F-test and write out your conclusion. Finally, complete an ANOVA summary table.

Reduced Model: $\qquad$

Full Model: $\qquad$

Omnibus F-Test: $\qquad$

| ANOVA |  |  |  |  |  |  | Mean Squares | F | Sig. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Source | Sum of Squares | df | M |  |  |  |  |  |  |
| Regression |  |  |  |  |  |  |  |  |  |
| Error |  |  |  |  |  |  |  |  |  |
| Total |  |  |  |  |  |  |  |  |  |


| Clerk | Days Absent | Attitude | Experience |
| :---: | :---: | :---: | :---: |
| 1 | 1 | 1 | 1 |
| 2 | 0 | 2 | 1 |
| 3 | 1 | 2 | 2 |
| 4 | 4 | 3 | 2 |
| 5 | 3 | 5 | 4 |
| 6 | 2 | 5 | 6 |
| 7 | 5 | 6 | 5 |
| 8 | 6 | 7 | 4 |
| 9 | 9 | 10 | 8 |
| 10 | 13 | 11 | 7 |
| 11 | 15 | 11 | 9 |
| 12 | 16 | 12 | 10 |
|  |  |  |  |
| Mean | 6.25 | 6.25 | 4.92 |
| Std. Dev. | 5.68 | $\mathbf{3 . 9 3}$ | $\mathbf{3 . 1 2}$ |


|  | Correlations |  |  |
| :---: | :---: | :---: | :---: |
|  | Days Absent | Attitude | Experience |
| Days Absent | 1 | .950 | .890 |
| Attitude | .950 | 1 | .951 |
| Experience | .890 | .951 | 1 |

$$
R_{Y X_{1} X_{2}}^{2}=0.9037
$$

4) We're interested in determining if an employee's attitude impacts their attendance at work. Specifically, we'd like to see if the combination of attitude and experience is a significant predictor of absences (compared to no predictors). A computer calculates the following regression equation:

Absences $=-2.263+1.550($ attitude $)-0.239$ (experience)

Does the combination of 2 predictor variables in this model significantly predict absences? Write out the full and reduced models, run the omnibus F-test, and complete the ANOVA summary table.

Reduced Model: $\qquad$

Full Model: $\qquad$

Omnibus F-Test: $\qquad$

| ANOVA |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Source | Sum of Squares | df | Mean Squares | F | Sig. |  |  |
| Regression |  |  |  |  |  |  |  |
| Error |  |  |  |  |  |  |  |
| Total |  |  |  |  |  |  |  |

5) Using your results from the previous two pages, determine if attitude significantly adds to the predictive accuracy of our model. In other words, determine if attitude impacts absences after controlling for experience.

Write out the full and reduced models, run the omnibus F-test, complete the ANOVA summary table, and write out conclusions.

Full Model: $\qquad$

Reduced Model: $\qquad$

Omnibus F-Test: $\qquad$

| ANOVA |  |  |  |  |  |  |  | Mean Squares | F | Sig. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Source | Sum of Squares | df |  |  |  |  |  |  |  |  |
| Exp \& Att |  |  |  |  |  |  |  |  |  |  |
| Attitude \| Exp |  |  |  |  |  |  |  |  |  |  |
| Error |  |  |  |  |  |  |  |  |  |  |
| Total |  |  |  |  |  |  |  |  |  |  |

What is $R_{Y X_{2} \mid X_{1}}^{2}$ ? $\qquad$

What is $\operatorname{SSReg}_{\mathrm{X}_{2} X_{1}}-\operatorname{SSReg}_{X_{1}}$ ?

