These methods require the assumptions of normality and equal variances

| Question | Observe | Method | Distribution | Standard Error |
| :---: | :---: | :---: | :---: | :---: |
| Does a group average differ from a hypothesized value? <br> Do cars on I-80 go faster than the 70 MPH speed limit? | $\bar{X}$ <br> Average speed from a sample of $n$ cars. | z-test <br> ( $\sigma$ is known) <br> t-test ( $\sigma$ is unknown) | If we repeatedly sample n observations and calculate $\bar{X}$, the distribution will approximate: <br> Z or t -distribution with $\mathrm{n}-1 \mathrm{df}$ | $\hat{\sigma}_{\bar{X}}=\frac{\sigma}{\sqrt{n}}$ $\hat{\sigma}_{\bar{X}}=\frac{s}{\sqrt{n}}$ |
| Do two independent group means differ? <br> Do male students write better essays than female students? | $\bar{X}_{1}-\bar{X}_{2}$ <br> Average essay rating for males and for females. | t-test | If we repeatedly sample $n$ observations and calculate $\bar{X}_{1}-\bar{X}_{2}$, the distribution will approximate: <br> t-distribution with $n_{1}+n_{2}-2 \mathrm{df}$ | $s_{\text {pooled }}=\sqrt{\frac{1}{n_{1}}+\frac{1}{n_{2}}} \sqrt{\frac{\left(n_{1}-1\right) s_{1}^{2}+\left(n_{2}-1\right) s_{2}^{2}}{n_{1}+n_{2}-2}}$ |
| Do two dependent group means differ? (matched pairs) <br> Do student scores increase from pretest to posttest? | $\bar{D}=\bar{X}_{1}-\bar{X}_{2}$ <br> Difference between avg. preand post-test scores. | t-test | If we repeatedly sample n observations and calculate $\bar{D}$, the distribution will approximate: <br> t -distribution with $\mathrm{n}-1 \mathrm{df}$ | $\hat{\sigma}_{\bar{D}}=\frac{s_{D}}{\sqrt{n}}$ |
| Does a group proportion differ from a hypothesized value? <br> Suppose the national smoking rate for men is $25 \%$. Does the smoking rate for Iowa differ from the national percentage? | $\mathrm{p}=$ proportion <br> Sample proportion of Iowans who smoke. | z-test | If we repeatedly sample $n$ observations and calculate $p$, the distribution will approximate: <br> Z distribution | $S E(p)=\sqrt{\frac{p(1-p)}{n}}$ |
| Do two group proportions differ? <br> Do more males or females vote Republican? | $\mathrm{p}=$ proportion <br> Sample proportions of males and females who vote Republican | z-test | If we repeatedly sample n observations and calculate the difference in proportions, the distribution will approximate: <br> Z distribution | $S E\left(\hat{p}_{1}-\hat{p}_{2}\right)=\sqrt{\frac{n_{1} \hat{p}_{1}+n_{2} \hat{p}_{2}}{n_{1}+n_{2}}\left(1-\frac{n_{1} \hat{p}_{1}+n_{2} \hat{p}_{2}}{n_{1}+n_{2}}\right)\left(\frac{1}{n_{1}}+\frac{1}{n_{2}}\right)}$ |


| Question | Observe | Method | Distribution |
| :--- | :---: | :---: | :---: | :---: |
| Does a group variance differ <br> from a hypothesized value? <br> Is this new measurement <br> procedure more precise than <br> industry standards? <br> Variance in measurement <br> for the new procedure. | $\chi^{2}$-test |  | Standard Error |

